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**Continuous selections for the metric projection on  $C_1$ .**

Constructive Approximation 4, No. 1, 85-96 (1988).

Let  $U$  be a finite dimensional subspace of  $C_1(K)$ , the continuous functions normed with the  $L_1$  norm.  $K$  is a compact subset of  $R^n$  and equal the closure of its interior. This paper proves that there is a continuous selection for the metric projection onto  $U$  only in the trivial case that  $U$  is a Chebyshev set. This tidy theorem for such a basic setting well supplements the few similar results in the literature for other spaces. In fact it is shown that if  $K$  is connected there does not exist a selection,  $s$ , for the metric projection such that even  $f_n$  converging uniformly to  $f$  does not mandate the convergence of  $s(f_n)$  to  $s(f)$ . The proofs involve a series of lemmas manipulating the characterization of best approximations in  $C_1(K)$  and the substructures forced upon  $U$  by the existence of a continuous selection for the metric projection. *D. Wulbert*

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